

(5)

∴ Solution of I.V.P.

$$y = \frac{1}{x^5} + \frac{2}{x} - \frac{1}{x} + \frac{4 \ln x}{x} = \frac{1}{x} + \frac{1}{x^5} + \frac{4 \ln x}{x}$$

4(a)

(18)

$$\mathcal{L}\{\sin(3t)\} = \frac{3}{s^2+9} \Rightarrow \mathcal{L}\{e^{-2t}\sin(3t)\} = \frac{3}{(s+2)^2+9}$$

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Now

$$\mathcal{L}\{t \sinh t\} = -\frac{d}{ds} \left\{ \frac{1}{s^2-1} \right\} = \frac{2s}{(s^2-1)^2}$$

$$\therefore \mathcal{L}\left\{ \int_0^t \tau \sinh \tau d\tau \right\} = \frac{2}{(s^2-1)^2}$$

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$$\text{Thus } \mathcal{L}\left\{ e^{-2t}\sin(3t) + \int_0^t \tau \sinh \tau d\tau \right\} = \frac{3}{(s+2)^2+9} + \frac{2}{(s^2-1)^2}$$

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